

# Towards Haptic Images: a Survey on Touchscreen-Based Surface Haptics

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**Abstract**—The development of tactile screens opens new perspectives for co-located image and haptic rendering, leading to the concept of “haptic images”. They emerge from the combination of image data, rendering hardware, and haptic perception. This enables one to perceive haptic feedback while manually exploring an image. This raises nevertheless two scientific challenges, which serve as thematic axes of the state of the art in this survey. Firstly, the choice of appropriate haptic data raises a number of issues about human perception, measurements, modeling and distribution. Secondly, the choice of appropriate rendering technology implies a difficult trade-off between expressiveness and usability.

**Index Terms**—survey, haptics, surface, touchscreen, image, texture.

## I. INTRODUCTION

**C**ONCURRENTLY to the spreading of touchscreens, the interest in their haptic enhancement grew, and became a new research field called “surface haptics”. Surface haptics refers to any system actuating a physical surface in order to produce haptic effects, preferably on the bare finger [1]. In the scope of this paper, we are mainly interested in the haptic rendering of images on touchscreens. We refer to this concept as “haptic images”. Therefore, we will narrow this survey on surface haptics systems which provide a co-located visuo-haptic feedback. The considered images can be 2D pictures as well as virtual objects in a 3D scene.

The premises of haptic images were laid with the concept of shape changing surfaces [2]. Ambitious attempts were made to mechanically actuate a surface in order to reproduce any shape in an interactive manner (see Section III-D). With the help of video projection, these displays provide co-localized shape and visual information. In these approaches, the resolution of the rendering is directly linked to the (high) density of actuators, resulting in a very expensive system.

The rise of tablet computers brought a new perspective to haptic images. They are highly integrated devices, combining touch tracking and visual display, in addition to self-contained battery power and operating system to run software. Therefore, it became very advantageous to use them as part of a haptic rendering setup. For instance, force-feedback arms or robotic systems were used to actuate directly a touchscreen, and provide it with force and motion abilities [3]. Most efforts in surface haptics have been concentrated on generating various types of vibrations that can alter the physics of the finger sliding on the screen, providing friction forces and even small relief sensations [4], [5]. Some alternative approaches made

use of an intermediate proxy acting on the finger with minimal sight obstruction [6]. Also, crossmodal effects like pseudo-haptic feedback can elicit haptic percepts without the need of a haptic actuator [7].

Figure 1 summarizes the scientific topics and challenges haptic images are related to. The conception of haptic images addresses image data, rendering hardware, as well as human haptic perception of surfaces. In this survey, we do not consider the issues related to image acquisition and rendering, which are broadly discussed in the literature. The concept of haptic images raises nevertheless two scientific challenges.

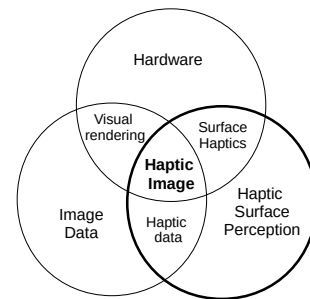


Fig. 1. Scientific fields and technical challenges for haptic images. The scope of the survey falls into the circle in bold.

Firstly, the general-case formalization of haptic data is not achieved yet. Surprising as it may seem, the very definition of the haptic properties of a material remains nowadays an open research question. Even in the engineering industry, there is no standard procedure (except for very specific contexts) to measure a set of properties needed to describe a material haptically.

Secondly, haptic rendering requires a set of technologies that can be complex to deploy. Covering a wide range of haptic sensations usually implies heavy technologies which are not likely to meet to consumer market. In order to get an interesting trade-off between technical complexity and expressiveness of the rendering, the development of haptic technologies requires to take into account perceptual factors and to focus on the most meaningful elements of haptic phenomena. As stated by Chang et al., “haptics are best employed when minimal actuation can have broad and great effect” [8].

## II. HAPTIC DATA: PERCEPTION, MEASUREMENTS, MODELING AND DISTRIBUTION

The use of haptic data can be an issue to achieve haptic rendering. Haptic rendering is the production of sensory stimuli in response to user interactions in order to produce one or

several haptic sensations (such as shape, compliance, friction, etc...) [9], [10]. While some systems are able to produce realistic sensations from simple mathematical heuristics, others make use of real-world measurements. Yet, haptic features are often tricky to characterize, and there is no standard way of measuring them, because there are no generalized definitions for them. Given the complexity of describing a subjective haptic experience, on which data should haptic simulation rely?

#### A. The challenge of haptic data: formalizing haptic properties

Every day, we touch and manipulate a large variety of materials, that we usually distinguish easily without the need of looking at them: our tactile sensitivity allows us to discriminate almost instantly a soft and sticky rubber from a cold and smooth metal or a harsh and dry textile. If identifying an object among others in a box can take only a few seconds [11], verbalizing the criteria on which we rely is much less spontaneous. In fact, there is no generic set of descriptors (verbal or not) to classify materials haptically. For instance, Yoshida had a quite wide approach with 20 adjective pairs [12]. On the other hand, when reducing the scope to a specific family, like banknotes, only two features can suffice for an accurate discrimination [13].

Because of a lack of appropriate vocabulary, tactile sensations and material properties are named with identical words (like “roughness” or “hardness”), although they are totally different things. This confusing polysemy gets even worse in the engineering field, where despite precise and formal definitions, a property like “roughness” can be described by a dozen of parameters and measured by several different methods [14]. As they relate to both physical properties and perceptual phenomena, haptic properties find themselves at the intersection of several fields of study like psychophysics, contact mechanics or surface metrology. Each of these perspectives may contribute, for a part, to the definition of a given haptic property, but they often have conflicting terminology.

Thus, the haptic description of an object often relies on subjective and context-dependent choices, which impedes the scientific effort of merging analysis and results. There is a need to clarify on which features one relies on when we appreciate or compare surfaces through touch. This would help to design haptic experiences more nely and achieve better user performance and experience, but also to refine the conception of haptic rendering devices. Haptic images directly raise this issue, with the concept of a generic visuo-haptic data format.

Once a measurable haptic data is defined, the design and fabrication of custom sensors is often needed. Adequate sensors for haptic measurements tend to be technically complex and expensive to produce. Their use is diversified and aims at different goals, namely robotic manipulation, haptic evaluation, material identification or realistic haptic simulations. Because each one of these application contexts implies a different use of haptic data, they require very different haptic acquisition approaches.

In this section, we first address the complexity of haptic perception of surfaces and the attempts to formalize it. Then,

we review the different strategies used to produce haptic information from the capture of real objects features. We also address the question of haptic modeling and its reliance or not on haptic measurements. Finally, we review recent attempts of making haptic data publicly available, which might be a decisive element for the development of haptic images.

#### B. Semantic issues with haptic descriptors: the case of roughness

Because they relate both to physical features and perceptual phenomena, haptic properties easily cross multiple perspectives and fields of study. Their restriction to quantitative characteristics leads inevitably to some terminology conflict. The term “roughness” is probably the most illustrative case of this semantic complexity.

Roughness has been extensively studied in the haptic literature (see [15] for a review), and yet its definition varies widely between authors. Even excluding perceptual aspects, roughness as a physical property is not a simple concept and has a debatable definition (according to the ISO 4287:1997, a dozen of different parameters can be used to assess it). Across this variety of conceptions, what can be safely said is that roughness is a geometrical feature of a surface, which relates to some form of spatial frequency.

Regardless of the chosen definition for “physical roughness”, perceived roughness is supposed to vary in intensity according to the former. Perceived roughness has been first hypothesized to be a single quantity depending only on a few geometrical properties of the touched surface, but no convincing model was found despite considerable efforts [16], [17], [18], [19], [20], [21]. It was demonstrated later that the perceived roughness verbally expressed by different subjects would relate to different objective measurements [22]. This suggests that a plurality of perceptions is associated to the word “roughness”. In other words, roughness entails several components and is hardly reducible to a single scalar value.

Indeed, a distinction is commonly made between fine and macro-roughness, which was confirmed by several studies [23], [24], [25] many decades after it was hypothesized by Katz under the famous name of the “duplex theory” [26]. This theory states that fine and coarse asperities are mediated by two distinct perceptual mechanisms, the first one relying on contact vibrations and the second one involving spatial distribution of pressure. It was notably found that contact vibrations are necessary to perceive asperities under 1mm [25]. Costes et al. pointed out that the perceived roughness cannot describe

entirely the surface geometry, in particular bumps or holes features [27]. Interestingly, a similar distinction can be found in surface metrology (ISO 4287:1997), where surface deviations are split on both sides of a sampling frequency: “roughness” refers to high frequency components, while low-frequency components are designated as “waviness”.

In order to address such semantic issues, Okamoto et al. suggested to distinguish between different semantic layers: the perceived attributes of a material, which constitute the psychophysical layer, serve as an interface between the measurable physical properties of the material (the material layer),

and higher cognitive layers (affective and preferential) [28]. The psychophysical layer relates to the perceptual representation of the touched object, and defines the scope for perceptual dimensionality, which we will address hereafter.

### C. Haptic perception of surfaces

Haptic perception is part of the somatosensory system, which mediates sensations coming from the body tissues (like skin, muscles or viscera). Physical sensations originate from the nerve impulses sent by a variety of receptors, which are distributed in the body and are specific to each sensory system. These receptors are of different types, with various shape, constitution and distribution making them sensitive to specific stimulation. The receptors of the tactile sense fall into three categories: mechanoreceptors, thermoreceptors and nociceptors. Although temperature sensing can play a crucial role in tactile discrimination, mechanoreceptors are of higher interest in the present work, because from a technological perspective, surface haptics is much more prone to mechanical stimulation than thermal rendering. For more details regarding the characteristics of these receptors, we refer the reader to [29], [30], [31].

It was mentioned in more recent studies [36], [34]. In fact, there has been little common understanding for decades in haptic research about the dimensionality of touch perception. The notion of “tactile primary colors” has been proposed by Kajimoto et al., emphasizing the complementarity of the mechanical stimuli which the four types of skin mechanoreceptors are sensitive to [37], [38]. As an analogy with the correspondence between color receptors in the eye and the color decomposition into primary colors, they suggested that a tactile sensation could be decomposed in four elementary stimuli, which would be perceived in a relatively independent manner. Pacini corpuscles react to the vibrations of a rough rubbing, Meissner corpuscles detect the indentation or stretch changes due to contact pressure, Merkel complexes are sensitive to the indentation due to a rough texture, while Rufini endings are supposed to respond to shear deformations produced by adherence. However, this direct correspondence appears to be very simplistic: for instance it does not explain why hardness can be correctly estimated through tapping vibrations rather than squeezing pressure. It has been argued by that the central integration of tactile afferents in the primary somatosensory cortex does not reflect this submodalities decomposition, but rather higher-level neuronal representations of tactile features across different receptor types [39]. For instance, while the spatial pattern of SA-I activation accurately reflects the shape in contact with the finger, it has been shown that subjects were able to identify letters formed by vibrating patterns which activated RA-I and RA-II, but not SA-I afferents [40].

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Fig. 2. Types of receptors for the kinesthetic and the tactile sensory systems.

### D. Perceptual dimensionality of haptic surfaces

In daily life we touch many surfaces and in many cases, we can identify them in a second without the need of looking at them. On the other hand, it is sometimes hard to get a specific object out of the bottom of a bag without several trials and visual validation. What are the features on which our haptic representation of surfaces is based on?

This question has been addressed in a large body of studies (for a review, see [32]). While these studies are generally consistent about the two most discriminative features being roughness and stiffness (which definitions are variable though), the rest of their results are quite diversified, yet without strong contradictions. This can be explained by the fact that these studies vary a lot in terms of stimuli choice, psychophysical methods and mathematical methods [33]. Tiest and Kappers demonstrated that if many studies concluded in a 2- or 3-dimensions model, they were valid only for a quite limited range of materials and that more descriptors were required to accurately depict the diversity of real-world materials [34]. Although most studies do not even mention it, temperature appears to be a very discriminative feature [35]. Stickiness

Fig. 3. Semantic layers of touch-related experiences, from [28].

Considered in a broad sense, compliance refers to how the surface deforms, roughness relates to its geometrical features, and friction concerns the easiness of the sliding

against it. Yet, each one of these three reviews outlined the inspirations that have led to the development of haptic devices, and most of them seek for multimodal sensing. An exception is the work of Edwards et al. who had an original approach using an expensive microphone only for textural discrimination [57]. However, artificial fingers are not necessarily intended to capture data for realistic haptic rendering; they rather replace human hands for material classification tasks [15]. In particular, the “BioTac” sensor distinguished itself by featuring a thermal sensing ability, in addition to vibration and deformation [56].

#### E. From tactile sensing to haptic evaluation

Tactile sensing, defined as the measurement of “given properties of an object through physical contact between the sensor and the object” [44], was developed in the first place for teleoperation systems, because reflecting contact forces is crucial for manipulation performances [45]. Semi or fully automated robotic manipulation also has a crucial need for tactile sensing, for instance to address the challenge of maintaining the grasp of an object with unknown weight and friction coefficient. Yet, these applications were in practice limited to real-time force and torque sensing, and did not ambition any storage of information for later use [44]. However, in the late nineties, the alternative use of tactile sensors to evaluate haptic properties was considered, pointing out many applications in other fields like medicine (especially for tumor detection), cosmetics (for product evaluation), or food industry (for delicate handling and inspection) [44]. For a comprehensive historical review we refer the reader to Tiwana et al.’s review [46].

From that moment, the interest grew for devices able to haptically characterize an object, which is also much valuable for the field of realistic haptic rendering. The idea of “reality-based” haptic models spread widely during the 2000s, with the exemplary ACME system [47]. This robotic measurement facility could produce completely automated measurements and be controlled over the network. It included notably a laser range finder for shape acquisition, a stereo vision color system for reflectance acquisition, and a probe with a force and torque sensor for texture, friction and elasticity estimations.

However, a limitation of computer-controlled scanning systems is that they hardly reproduce the mechanical behavior of a human hand. Therefore, despite of their high reliability and reproducibility, they produce contact forces which differ from the one of natural human interaction. In this regard, several handheld probes were proposed instead [48], [49]. They measured contact forces and vibrations, and were usually combined with an optical position tracking system. Methods to map such surface measurements on a 3D mesh in an interactive manner were discussed in [50] and [51]. Battaglia et al. went even further and proposed thimble-shaped wearable sensors in order to measure multi-finger forces during grasping and manipulation [52].

#### F. Bio-inspired sensors and material classification

Artificial fingers constitute another trend for tactile sensor design [53], [54], [55], [56]. By mimicking the mechanical behavior of a human finger, they aim at reducing, as much as possible, the effect of artificial mechanical transductions which are typically induced with probes. Artificial fingers also

As machine learning techniques spread widely in almost all fields of science, the most recent trend in haptic acquisition is the treatment of unconstrained multimodal data. Gao et al. applied deep learning over both visual and haptic data to develop a prediction model for robots to anticipate contact with visible objects [58]. The “Proton Pack” is a handheld surface interaction recording system with an impressive number of sensors [59], [60], [61]. It is intended to produce an ambitious multimodal dataset for autonomous robots to properly interact with their environment. Another inspiring body of work in that domain is the one of Strese et al. who used audio signal analysis in conjunction with machine learning algorithms on both sound and acceleration data [62], [63]. One particularly interesting trait of their approach is that they put effort on establishing a ground truth about perceptual similarity from subjective psychophysical experiments, aiming at matching robotic analysis with the ve human perceptual dimensions [64], [65].

#### Explicit and implicit haptic modeling

Haptic data are not necessarily at the core of haptic rendering, but haptic modeling is. Haptic rendering can be considered as a relationship between given exploratory or manipulatory inputs and given delivered outputs. In this regard, it expresses a model of the contact phenomena.

The most straightforward approaches for rendering consist in using explicit models: approximating the virtual object by an idealized, simplified mathematical model in order to run a physical simulation. The quality and realism of the resulting experience is thus dependent on the proper choice of the physical parameters of the model. The typical example is the use of the Hooke’s law to simulate stiffness. Because of their simplicity, explicit models were popular in the beginnings of haptic rendering [66], [67], [68]. The parameters of the model can be eventually fitted through measurements done on real objects [69], [51], [70], [71], which is usually referred as “measurement-based modeling”. Explicit models have two main limitations. Firstly, they require some preliminary knowledge on the physical phenomena that are to be simulated. Secondly, outside of simplistic cases, they often require considerable sophistication to provide a convincing result, and can thus be unfit for the real-time rendering of complex, realistic scenes with non-linear behaviors [72].

More recently, “data-driven” approaches were proposed as an interpolation of sparse recordings of the real interaction [73], [74], [75], [76]. A strength of such implicit methods is to make use of precalculations on the recorded

data to provide sophisticated outcomes in real-time. In an approach tackles the difficulty of producing quality haptic pioneer contribution, Hover et al. proposed two of the force content in large and complex scenes, which is one of the main old interpolation schemes in order to render one-dimensional visco-elasticity [74]. Their method could handle arbitrary non-linear materials with visco-elastic behavior. This work was later extended to the rendering of viscous fluids [77], slipping phenomena [78], and inhomogeneous behaviors [79]. More recently, Costes et al. proposed a texture-based format to store ten haptic features [43]. It extends the concept of normal force or bump maps used in computer graphics to add the relief to 3D objects. Their textures can store friction, hardness, and temperature information that are mapped to 3D objects. Shin et al. Choi relied on photogrammetry to generate a high quality height map of set of textures [80]. Parametric models were used for friction and stiffness though (Dahl and Hunt-Crossley models respectively). Because of their promising possibilities in terms of real-time realistic rendering, data-driven approaches received great attention in the field of medical training and robotic surgery [81], [71].

#### H. Haptic databases

A few authors worked on constituting haptic datasets for use by the research community. They are listed in Table I. Publicly accessible databases save the research community time because collecting data can be time intensive and expensive. This ambition is quite recent, as the very first attempt was the one of Culbertson et al. [82]. They provided one hundred haptic texture and friction models, the recorded data from which the models were made, images of the textures, and the code and methods necessary for rendering on a commercially available device. Each texture and friction model was based on a ten-second freehand recording of the force, speed, and high frequency acceleration measured with an instrumented probe.

Shortly after, Strese et al. proposed a set of controlled and freehand acceleration recordings of 43 different textures [83]. Control recordings were done under two conditions, either with constant force and increasing scan velocity, or constant velocity and increasing normal force. Uncontrolled recordings consisted in a set of ten different twenty-second recordings following ve lateral movements and ve circular movements. The dataset was later extended to 69 textures, including measurements of sound, grasping force, and images [62]. The authors also provide on their website two others databases of 108 surface materials and 184 buildings materials.

The Proton Pack project envisions the constitution of a comprehensive multimodal dataset [61]. Because of the quantity of data it is able to gather, this work opens a lot of exciting possibilities and challenges in data treatment and analysis. Another ambitious recent work foresees a "universal haptic library"<sup>4</sup>, where psychophysical haptic features are matched with visual features, in order to automatically generate a haptic data-driven model from an unknown visual texture [73]. Such

### III. TECHNOLOGICAL SOLUTIONS FOR TOUCHSCREENBASED SURFACE HAPTICS

On a more materialistic perspective, one major limitation of haptic technologies is the technical complexity of mechanical actuators. If traditional force-feedback devices are effective for teleoperation and have been introduced in industrial and medical applications, they remain often complex, cumbersome and expensive. Adding more pieces of hardware to render more haptic properties will not help to spread this technology in the consumer market like touchscreens did.

A. The challenge of surface haptics hardware: lightweight but expressive

The challenge of simplicity applies to haptic technologies from their conception to their end-use, as its impact is considerable on both production costs and use case relevance. Usual vibrators embedded in cellphones and game controllers are a typical example of a successful simple technology, but their expressiveness is also remarkably limited. They illustrate on one hand the relevance of the haptic modality in many cases, and on the other hand the immense underuse of our haptic sensitivity.

Haptic researchers have proposed a number of innovative solutions in the recent years to provide haptic feedback and tactile sensations to touchscreens. Yet, most of these technologies provide only a limited range of tactile sensations, which depends largely on the generated stimulus. In order to address the full richness of haptic perception, several actuators could be combined to deliver specific stimuli of different kinds: forces, vibrations, shape and temperature. However the technical complexity of such a build-up can be huge.

Besides, it is noteworthy that an additional stimulus (for instance, shape in addition to forces) does not necessarily adds to the richness of the rendering. Before being transformed into a sensation, sensory cues are merged into a complex integration process [86], [87]. Hence, the quality and expressiveness of a haptic rendering is less due to the number of stimuli than to their congruence and complementarity; which is hard to evaluate directly. Some approaches can be used to estimate the optimal number of dimensions necessary to discriminate between samples, like multidimensional scaling [88]. They provide useful qualitative leads on the perceptual significance of each considered features, but do not provide definitive answers for the technical dilemmas of rendering technologies.

<sup>1</sup><http://haptics.seas.upenn.edu/index.php/Research/ThePennHapticTextureToolkit>

<sup>2</sup><https://zeus.lmt.ei.tum.de/downloads/texture/>

<sup>3</sup><https://alexburka.com/penn/proton.php>

<sup>4</sup><http://haptics.khu.ac.kr/the-haptic-library/>

<sup>5</sup><http://haptic.buaa.edu.cn/EnglishFabricDatabase.htm>

| Samples | Type             | Image                              | Data  | Capturing tool           | Explo. method          | Ref  |
|---------|------------------|------------------------------------|---|--------------------------|------------------------|------|
| 100     | various          | X                                  | 3DoF acceleration, force, position  | Haptographer             | Free hand              | [85] |
| 100     | various          | X                                  | AR coeff. (x100), HC coeff. (x30), Dahl coeff. (x22). Generated by model.   | Accel., force sensor     | Free hand              | [73] |
| 120     | fabric           | X                                  | Normal force, frictional force, friction coeff, displacement, velocity  | Custom device on nger    | Free hand              | [84] |
| 69      | surface material | + macro image                      | 3DoF accel, friction (2x FSR), metal detection, re ectance, sounds (sliding + tapping)  | Phantom Omni + Texplorer | Controlled + free hand | [62] |
| 108     | surface material | + macro image with and without ash | 3DoF accel, friction (2x FSR), metal detection, re ectance, sounds (sliding + tapping)  | Texplorer                | Free hand              | [62] |
| 184     | surface material | + macro image with and without ash | 3DoF acceleration (sliding+tapping), density, temperature, metal detection, sound (sliding+tapping), re ectance, FSR compliance, FSR friction | Texplorer2               | Free hand              | [62] |

TABLE I

HAPTIC DATABASES ASSOCIATING IMAGES TO HAPTIC DATA

In this section, we review solutions for the haptic enhance-Another technique, called electrovibration, consists in am- ment of touchscreens according to the type of actuation they imply. The vast majority of them is based on mechanical stimu- lation, and neglects thermal stimuli. This can be explained by the technical difficulty to combine tactile screen interactions with temperature control. Although some examples exist [89], they are non-colocated and were therefore considered as out of scope for our review. These solutions are summarized in Table II, and organized along Costes et al.'s perceptual dimensions (see Section II-D).

### B. Vibrotactile actuators

Because of their simplicity of integration, embedded vibrators are very common in nowadays mainstream tactile devices, and they tend to be intensively used for both gaming and GUI interactions enhancement. It is a fact that even a very simplistic haptic feedback can considerably increase the comfort and/or performance of tactile screen interactions (like the vibratory feedback when typing, for instance) [90]. However, the possibilities of usual embedded vibrators for haptic feedback remain limited: because they act on the whole screen as a single source, they produce a similar effect on different ngers touching the screen, and they cannot provide localized or moving stimuli. Furthermore, because they are generally simple eccentric rotors, they operate in a very narrow range of frequencies.

Many researchers have proposed creative ways to enrich touchscreens with an additional vibrator. The vibrator can be placed either on the nail [91], between several ngers and the screen [92], on the device [93], [94], [95] or both on the device and on haptic gloves [96]. In particular, Romano and Kuchenbecker used a high-quality one-dimensional vibrator to display compelling texture details through an actuated stylus, according to normal contact force and lateral speed [97].

### C. Variable friction displays

Vibrations can be used as a haptic signal mechanically transmitted to a nger; but they can also be a mean to modify the physical phenomena occurring on contact with a surface, particular, ultrasonic frequencies are able to produce a thin layer of air between the nger and the vibrating a surface, resulting in a diminished resistance to sliding. This friction reduction technique, first described by Watanabe and Fukui [98], was applied to touchscreens only in the 2010s [99], [100].

Another technique, called electrovibration, consists in applying electrostatic forces through high-voltage oscillations. Although the concept was dating back to the 1950s [102], Linjama and Mäkinen were the first to use it on a transparent substrate, compatible with a tactile screen [103]. In both approaches, friction can be modulated to produce texture effects and even 3D pattern features [4], [5]. Smith and Goblewicz combined both approaches on a single touchscreen to enlarge the range of simulated friction [104].

Planar force feedback rendering can be achieved with variable friction applied in an asymmetric way. For instance Chubb et al. applied in-plane oscillations to their device's friction pad while actively varying this pad's friction level to create directional shear forces [1].

### D. Shape changing screens

Shape changing screens, as their name indicates, intend to reproduce the shape of an object consistently to its visual display. A pioneer work in that field is the FEELEX project [2], a deformable 24cmx24cmx3mm plane actuated by an array of thirty six linear actuators. Each actuator is combined with a force sensor, providing interaction with the graphics which are projected on the surface from the top. Since then, a variety of other technological solutions have been proposed to achieve a similar concept. The main technical challenge for shape changing screens is to achieve acceptable performances for both resolution and actuation latency, with a limited bulkiness. Jansen et al. used electromagnets and magnetorheological fluids to achieve low-latency multitouch feedback, at the cost of a low resolution [105]. In contrast, Fuller et al.'s Tunable Clay is a malleable screen with a hydraulic-activated particle jamming controlling its global stiffness [106]. Leithinger et al. proposed a solution with simplified open-source hardware and no sensors in order to make it scalable and affordable [107]. In particular, the MIT Media Lab did an impressive work in designing a variety of pin-based shape displays and exploring their many applications, like UI dynamic affordance, physical rendering, 3D model manipulation, physical telepresence, music computing [108], [109], [110], [111]. Siu et al. extended the concept with a mobile tabletop display [112]. They designed a 288 actuated square pin array, mounted on a mobile platform. Relying on an optical tracker, the device is able to follow one's hand watching a surface within a VR headset.

## E. Moveable touchscreens

As an alternative to the technical complexity of shape-changing screens, it can be beneficial to actuate a regular touchscreen with a robotic system providing motion and/or force-feedback abilities. By doing so, one takes advantage of the highly integrated nature of touchscreens, namely a high-resolution visual display with co-localized touch tracking. Yet, only a few solutions were proposed to haptically enhance a touchscreen with motion.

The “TouchMover” device is a touchscreen actuated and moved using force-feedback in the normal direction [113]. The second version includes vibrators that allows to render either fine shape details or local content information [114]. Another approach presented by Takanaka et al. consists in a touchscreen with planar force-feedback and large translation and rotation abilities, simulating contact, inertia, shape and stiffness [115]. In a way similar, Costes et al. proposed “KinesTouch”, a tablet computer mounted on a 3DoF force-feedback device [27]. In addition to shape, compliance, friction and fine roughness of a surface can be simulated.

Rotational movements can also be used to express the curvature of a virtual object on contact point, as proposed by Kim et al. [116]. Parallel platforms are an efficient way to provide this inclination feedback, as shown in the work of Maiero et al. [117] and Hausberger et al. [3].

## F. Actuated proxies

Instead of actuating the touchscreen itself, several authors proposed to make use of an intermediate part. Most of these solutions can be classified along three categories: the one providing a proxy just under the finger, the one actuating a transparent overlay covering the screen, and the one acting on the back of a handheld device in a pseudo-colocated way. We will not address here the many works involving actuated probes (stylus, pen, stick, etc...), as they imply rather different types of interaction than touching the screen with the finger pad.

Portillo et al. proposed to use a pantograph above a touchscreen for multimodal handwriting and drawing assistance [118]. Yang et al. had an original approach with a 4-DoF string-based system actuating two digital rings and providing grasp force-feedback [119]. The system was adapted later on a handheld tablet, with a single ring, in order to provide 2.5D geometry and texture feedback [120], [6]. The “FingerFlux” uses electromagnetic actuation on a permanent magnet placed under the finger [121]. It achieves attraction, repulsion, vibration, and directional haptic feedback on and near the surface, perceivable at a distance of several centimeters. Finally, the “HapticLens” is a transparent “tangible” allowing to feel the stiffness of any region of an image [106]. The hydraulic jamming system controls the density of the chamber, going from liquid to solid consistency.

Some authors suggested to actuate a transparent film covering the whole screen. Wang et al. demonstrated a 2-DoF translational motion “Haptic Overlay Device”, intended to enhance GUI interactions on automobile dashboards [122]. The inspiring work of Roudault et al. in particular, investigated

the uses of a tactile gesture output [123]. Their two prototypes could guide the finger on the screen to reproduce a given gesture like a letter or a symbol, without the need of looking at it. Another approach is the one of Kajimoto who proposed a transparent electro-tactile display for active multi-touch shape feedback [124].

Finally, the “back-of-device approach” is a canny workaround for occlusion problems. Assuming the touchscreen is handheld, the position of a fingertip on its back side can be perceptually associated with the position of touch input on the screen. Force feedback [125] or electro-tactile feedback [126] can be provided to a holding finger on its back side, in reaction to thumb touch inputs. In contrast, Kokobun et al. used the back side as a touch input to showcase visual pseudo-haptic effects without occlusion [127].

## G. Pseudo-haptic feedback

“Pseudo-haptic feedback” refers to a non-haptic feedback inducing or modifying a haptic sensation in response to a force or motion input. Its very first use was to replace expensive haptic devices with passive ones [134]. The first contributions on the topic mostly relied on modifying the Control / Display (C/D) ratio of the mouse cursor in order to generate the feeling of going through a bump or a hole. Additional works explored other haptic properties such as shape for stiffness, speed for friction or mass, trajectory for slope (for a review, see [134]).

In the following decade, alternative approaches were explored. Keller et al. induced “pseudo-weight” sensations in drag interactions by making object harder to displace [135]. Watanabe changed the C/D ratio of a scrolling background image instead of the cursor to induce friction sensations [128]. The “Elastic Image” proposed by Argelaguet et al. consists in deforming an image being clicked locally [129]. The progressive deformation (which approximately substitute pushing force by time) creates a quantitative softness sensation. With a similar visual effect, Punpongsanon et al. used video-projection and finger-tracking to enhance the perceived softness of a real object [136]. Ban et al. used visual retargeting to provide illusory shape curvatures [137]. Only a few authors applied pseudo-haptic principles to touch interactions. Some of them chose a non-colocated approach, to avoid occlusion and decoupling issues [138] [127] [139].

Other authors leveraged co-localized touch interactions to display pseudo-haptic effects on touchscreens. Ridzuan et al. changed the visual aspect of the user's finger according to the applied pressure to simulate variable stiffness [130]. The approach of Watanabe was adapted to touchscreens in [131] and [132], inducing quantitative sliding sensations. Fleureau et al. adapted the Elastic Image technique to a tactile tablet, with an additional audio feedback to simulate roughness [7]. Costes et al. relied on a deformable cursor between the user's finger and a tablet computer to provide pseudo haptic sensations of hardness, friction, fine roughness, and macro roughness [133].

## IV. DISCUSSION AND CONCLUSION

The concept of haptic images constitute a pragmatic entry point for major scientific challenges of tomorrow's haptics

| Approach              | Technology                              | Ref.                 | Compliance | Friction | Shape | Roughness |
|-----------------------|---|----------------------|------------|----------|-------|-----------|
| Vibrotactile          | Vibrations                              | ActiveClick [90]     | X          |          |       |           |
| Vibrotactile          | Finger-mounted vibrations               | [91]                 |            |          | X     |           |
| Vibrotactile          | Finger-mounted vibrations               | [92]                 |            |          | X     |           |
| Moveable screen       | 1DoF Normal force-feedback              | TouchMover [113]     |            |          | X     |           |
| Moveable screen       | 1DoF Normal force feedback + vibrations | TouchMover 2.0 [114] | X          |          | X     |           |
| Moveable screen       | 2DoF Lateral force feedback             | [115]                | X          |          | X     |           |
| Moveable screen       | 3DoF force feedback                     | ForceTab [117]       |            |          | X     |           |
| Moveable screen       | 3DoF force feedback                     | Kinestouch [27]      | X          | X        | X     | X         |
| Moveable screen       | 3Dof Rotational force-feedback          | [116]                |            |          | X     |           |
| Moveable screen       | 3Dof Rotational force-feedback          | Surtics [3]          |            |          | X     |           |
| Shape changing screen | Pin Array                               | Feelex [2]           |            |          | X     |           |
| Shape changing screen | Pin Array                               | Reief [107]          |            |          | X     |           |
| Shape changing screen | Pin Array                               | inFORM [109]         |            |          | X     |           |
| Shape changing screen | Pin Array                               | ShapeShift [112]     |            |          | X     |           |
| Shape changing screen | Array electromagnet + MR uid            | MudPad [105]         | X          |          | X     |           |
| Shape changing screen | Hydrolic jamming system                 | Tunable clay [106]   | X          |          | X     |           |
| Actuated proxy        | Cable proxy                             | FingViewer [119]     |            |          | X     |           |
| Actuated proxy        | Cable proxy                             | [120]                |            |          | X     |           |
| Actuated proxy        | Cable proxy                             | [6]                  |            |          | X     | X         |
| Actuated proxy        | Finger-mounted magnet                   | FingerFlux [121]     | X          |          |       |           |
| Variable friction     | 2DoF Lateral force feedback             | longRangeOuija [123] |            | X        |       |           |
| Variable friction     | Ultrasonic friction reduction           | TPad [5]             |            | X        |       |           |
| Variable friction     | Ultrasonic friction reduction           | LATPad [99]          |            | X        |       |           |
| Variable friction     | Ultrasonic friction reduction           | Tpad Fire [100]      |            | X        | X     |           |
| Variable friction     | Electrostatic friction amplification    | TeslaTouch [101]     |            | X        |       |           |
| Variable friction     | Electrostatic friction amplification    | TeslaTouch [4]       |            |          | X     |           |
| Variable friction     | Electrostatic friction amplification    | E-sense [103]        |            | X        |       |           |
| Pseudo-haptics        | C/D ratio                               | [128]                |            | X        |       |           |
| Pseudo-haptics        | C/D ratio                               | Elastic image [129]  | X          |          |       |           |
| Pseudo-haptics        | C/D ratio                               | [130]                | X          |          |       |           |
| Pseudo-haptics        | C/D ratio                               | [131]                |            | X        |       |           |
| Pseudo-haptics        | C/D ratio                               | [132]                |            | X        |       |           |
| Pseudo-haptics        | C/D ratio                               | Touchy [133]         | X          | X        |       | X         |
| Pseudo-haptics        | C/D ratio + audio                       | [7]                  | X          |          |       | X         |

TABLE II

SURFACE HAPTIC DEVICES ASSOCIATED TO A TACTILE DISPLAY THEY ARE CLASSIFIED ALONG COSTES ET AL PERCEPTUAL DIMENSIONS [27].  
ROUGHNESS ENCOMPASSES FINE AND MACRO ROUGHNESS AND WARMTH IS NOT CONSIDERED HERE

techniques. Firstly, the formal definition of haptic properties is not mature enough to lead to a generic haptic formalism. Secondly, despite very creative research efforts to develop haptic hardware, the trade-off between expressiveness and usability remains a difficult choice. Thus, this paper provided a literature review in perspective of these two major topics.

The perceptual mechanisms of haptic interactions with surfaces were presented and discussed. While skin mechanoreceptors show specific sensitivities to various tactile features, the choice of descriptors to quantify a haptic experience remains an open question. The experimental evaluation of haptic sensations is easily scrambled by semantic issues. If they can be classified along four general perceptual dimensions, namely compliance, roughness/geometry, friction and warmth, there is a need for a more precise typology. There is room for more sophisticated psychological research, notably to compare different modalities providing the same percept.

We provided an overview of previous solutions for touch-screen haptic enhancement, which span a variety of technological approaches: vibrotactile feedback, variable friction displays, shape changing screens, moveable touchscreens, or actuated proxies. Regardless of their technical complexity, most of them address a limited range of sensations. Cross-modal effects like pseudo-haptic feedback can also complement haptic feedback without the need of a haptic actuator. Eventually, the concept of haptic images will follow the evolution of image displays towards haptic holography [141].

Beside the problem of matching human sensations, defining the resolution of image displays towards haptic holography [141].



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